



UNIVERSIDAD NACIONAL AUTÓNOMA DE MÉXICO  
PROGRAMA DE POSGRADO EN  
FILOSOFÍA DE LA CIENCIA

UNAM  
POSGRADO

<b>Actividad Académica:</b> STS FMLC Introducción a la Lógica Paraconsistente			
<b>Clave:</b>	Semestre: 3	<b>Campo de conocimiento:</b> FMLC	
<b>Carácter:</b> Obligatoria ( ) Optativa ( ) de Elección ( )		<b>Horas por semana</b>	<b>Horas al semestre</b>
<b>Tipo:</b>	Teóricas: 4	Prácticas:	No. Créditos: 8
<b>Modalidad:</b> Presencial		<b>Duración del programa:</b> 1 semestre	

**Seriación:** Si ( ) No ( X )      **Obligatoria** ( X )      **Indicativa** ( )

**Introducción:** Classical logic does not tolerate contradictions—deriving a single inconsistency from a given classical theory allows for anything else to be thereby derived. Paraconsistent logics are more resistant to such contamination—whether a contradiction arises in the scope of a discourse or a discussion, or happens to follow from the information contained in a database, it is often worth identifying it, isolating it, or somehow controlling its potentially harmful effects.

**Objetivo general:** This course will provide an introduction to paraconsistency, from an abstract, a semantical and a deductive viewpoints, with an emphasis on recent (15 years or less) developments.

Contenido Temático			
Unidad	Temas	Horas	
		Teóricas	Prácticas
1	What is a Paraconsistent Logic? 1.1 Inconsistent-tolerant logics are introduced and discussed. 1.2 Will we contradict ourselves?	4	0
2	Genuine Paraconsistency 2.1 Is the invalidity of Explosion enough for paraconsistency, or something else is required? 2.2 Can the Law of Non-Contradiction be valid in a paraconsistent logic?	4	0
3	What is Negation?	4	0

	3.1 The nature of negation. 3.2 Are we still talking about negation when considering a connective that fails the Principle of Explosion?		
4	Logics of Formal Inconsistency  4.1 Internalizing at the object language the metatheoretical notion of consistency. 4.2 How can we recover classical reasoning from within a non-classical environment?	4	0
5	Other recovery strategies  5.1 Other mechanisms for recovering classical reasoning from within a non-classical environment.	4	0
6	Interlude on duality: paraconsistency and paracompleteness  6.1 What are the relations between paraconsistent logics and constructive logics?	4	0
7	Multi-valued semantics – the deterministic case  7.1 What are the advantages and disadvantages of dealing with 3-valued and 4-valued non-classical negations?	4	0
8	Multi-valued semantics – the non-deterministic case  8.1 Beyond truth-functionality. 8.2 What other kinds of finite-valued paraconsistent negations are there?	4	0
9	Worlds semantics  9.1 Negations with a modal character. 9.2 How best to understand negative modalities?	4	0
10	A proof theory for negative modalities  10.1 Sequent calculi for negation as negative possibility (and for negation as impossibility). 10.2 What are their main properties?	4	0
11	Paraconsistency, meta-paraconsistency and beyond	4	0

	11.1 Metaentailments: Transitivity and Monotonicity are examples of such meta-entailments. 11.2 What does paraconsistency look like in such a setting?		
12	Contradictory logics 12.1 Are there sensible cases of contradictory logics?	4	0
13	Inconsistent mathematics 13.1 A set belonging and not belonging to itself. 13.2 What other mathematical creatures could one find if Mathematics is done paraconsistently?	4	0
14	Inconsistent semantics 14.1 Can an argument be both valid and invalid?	4	0
15	Mini-seminar on paraconsistent logics	4	0
16	Mini-seminar on paraconsistent logics	4	0
<b>Total de horas:</b>		64	0
<b>Suma total de horas:</b>		64	

### Bibliografía y actividades:

**Nota:** Although the course is intended to be taught in Spanish, it may include some sessions in English.

Medios didácticas:	Métodos de evaluación:
Exposición profesor(a) (X)	Exámenes o trabajos parciales (X)
Exposición alumnos (X)	Examen o trabajo final escrito ( )
Ejercicios dentro de clase (X)	Trabajos y tareas fuera del aula (X)
Ejercicios fuera del aula (X)	Exposición de alumnos ( )
Lecturas obligatorias (X)	Participación en clase (X)
Trabajo de investigación (X)	Asistencia (X)
Prácticas de campo ( )	Prácticas ( )
Otros: _____ ( )	Otros: _____ ( )

### Evaluación y forma de trabajo

Aattendance (10%), participation in classes and mini-seminars (40%), periodic written assignments (50%). Handout and slides will be self-contained, but additional reading material will be offered to the students according to their specific interests.

**Imparten:** João Marcos (UFSC, IIFs) y Luis Estrada-González (IIFs)

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### Día y hora del curso o seminario:

Viernes de 10:00 a 14:00

### Bibliografía mínima (puede cambiar)

Carolina Blasio, Carlos Caleiro y João Marcos. What is a logical theory? On theories containing assertions and denials. *Synthese*, 198:5481–5504, 2021.

Guillermo Badia y João Marcos. On classes of structures axiomatizable by universal d-Horn sentences and universal positive disjunctions. *Algebra Universalis*, 79(41), 2018.

Carolina Blasio, João Marcos y Heinrich Wansing. An inferentially many-valued two-dimensional notion of entailment. *Bulletin of the Section of Logic*, 46(3/4):233–262, 2017.

Alexander Bochman. Biconsequence relations: A four-valued formalism of reasoning with inconsistency and incompleteness. *Notre Dame Journal of Formal Logic*, 39(1):47–73, 1998.

Carlos Caleiro, Sérgio Marcelino y João Marcos. Merging fragments of classical logic. In *Frontiers of Combining Systems: 11th International Symposium, FroCoS 2017, Proceedings*, volume 10483 of *LNCS*, Springer, pages 298–315, 2017.

Carlos Caleiro, Sérgio Marcelino y João Marcos. Combining fragments of classical logic: When are interaction principles needed? *Soft Computing*, 23(7):2213–2231, 2019.

Jon Michael Dunn y Gary Hardegree. *Algebraic Methods in Philosophical Logic*. OUP Oxford, 2001.

Vitor Greati y João Marcos. Finite Two-Dimensional Proof Systems for Non-finitely Axiomatizable Logics. In: *Automated Reasoning: IJCAR 2022, Proceedings*, volume 13385 of *LNCS*, pages 640–658. Springer, 2022.

Vitor Greati, Sérgio Marcelino y João Marcos. Proof search on bilateralist judgments over non-deterministic semantics. In *30th International Conference on Automated Reasoning with Analytic Tableaux and Related Methods (TABLEAUX 2021), Proceedings*, volume 12842 of *LNCS*, pages 129–146. Springer, 2021.

Lloyd Humberstone. Heterogeneous logic. *Erkenntnis*, 29(3):395–435, 1988.

Ian Rumfitt. 'Yes and No'. *Mind*, 109(436):781–823, 2000.

D. J. Shoesmith y Timothy John Smiley. *Multiple-Conclusion Logic*. CUP, 1978.

Yaroslav Shramko y Heinrich Wansing. *Truth and Falsehood: An inquiry into generalized logical values*. Springer, 2011.

Ryszard Wójcicki. *Theory of Logical Calculi*. Kluwer, Dordrecht, 1988.